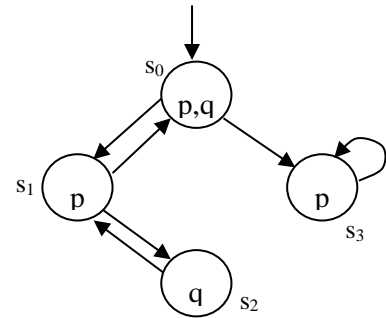


1. Given a transition system  $M = (S, S_0, L, R)$  (in the figure),  
 i) complete the specification of  $M$  by substituting "..." with right symbols according to the figure;

$S = \{s_0, \dots, s_3\}$   
 $S_0 = \{s_0\}$   
 $L : \quad l(s_0) = \{p, q\},$   
 $\quad \quad l(s_1) = \{p\}$   
 $\quad \quad l(s_2) = \{\dots\} \dots\dots\dots$   
 $\quad \quad l(s_3) = \{\dots\} \dots\dots\dots$   
 $R = \{ \langle s_0, s_1 \rangle, \dots \}$



- ii) Specify the transition relation  $R \equiv \bigvee_{i,j} R_{i,j}$  of model  $M$  in symbolic form where  $R_{i,j}$  specifies an individual transition, e.g.  $R_{2,1} \equiv \neg p \wedge q \wedge p' \wedge \neg q'$ . Try to simplify  $R$  if possible.
- iii) Find the states of  $M$  where following CTL formulas hold:

- a)  $AX(p)$  .....
- b)  $EG(p)$  .....
- c)  $\neg AG(p)$  .....
- d)  $EF EG(p)$  .....
- e)  $A(p U q)$  .....

2. Express the formulas below using minimal set of CTL operators EX, EG, EU and  $\neg$ :
- i.  $AX(p)$  .....
  - ii.  $EF(p)$  .....
  - iii.  $\neg AG(p)$  .....

3. Given a symbolic state:  $\varphi \equiv x_1 \wedge \neg x_2$  and transition relation  $R \equiv x_1 \wedge x_2 \wedge \neg x_1' \vee \neg x_2'$ . Find symbolic pre-image  $EX(\varphi)$  of  $\varphi$ . For this, use the definition  $EX(\varphi) \equiv \exists V' (R \wedge \varphi[V' / V])$  and  $\exists$ -quantifier elimination for simplification.

4. Draw a cyclic Uppaal process with total duration within interval  $[d_1, d_2]$  and which is started with initial synchronization via channel  $ch$ .